

Unit I

Digital computers and digital systems: binary numbers, Binary addition and Subtraction, Unsigned Binary numbers, 1's compliments, 2's compliments, Number base conversion, Octal and Hexadecimal number system, Compliments, Binary codes, Binary storage and Registers. Algebra: Definition of Boolean Algebra, Laws and Theorems and properties of Boolean algebra, Simplifications of Boolean functions for 2, 3 and 4 variable maps, Sum-of-products, product of sums, Karnaugh Map, menthol Canonical forms, Don't Care conditions.

Binary Numbers:

Representation: Binary numbers use only two digits, 0 and 1, to represent all values.

Place Value: Each digit's position represents a power of 2 (similar to how decimal positions represent powers of 10).

Conversion: Converting from decimal to binary involves division by 2 and noting remainders.

Binary Addition and Subtraction:

Addition: Adding binary numbers follows the same rules as decimal addition but with simpler carry rules ($0 + 0 = 0$, $1 + 0 = 1$, $1 + 1 = 10$).

Subtraction: Subtraction in binary involves borrowing, similar to decimal subtraction.

Unsigned Binary Numbers:

Representation: Positive integers are represented in binary without a sign bit.

1's Complement:

Representation: To represent negative numbers, invert all the bits of the corresponding positive number.

Addition: Add 1 to the least significant bit to convert between positive and negative numbers.

2's Complement:

Representation: To represent negative numbers, invert all bits and add 1 to the least significant bit.

Advantages: Provides a unique representation for zero and simplifies arithmetic operations.

Number Base Conversion:

Binary to Decimal: Multiply each digit by its place value and sum the results.

Decimal to Binary: Successively divide the decimal number by 2, noting remainders.

Octal and Hexadecimal Number Systems:

Octal (Base 8): Uses digits 0-7 to represent binary numbers in groups of 3 bits.

Hexadecimal (Base 16): Uses digits 0-9 and A-F to represent binary numbers in groups of 4 bits.

Complements:

Used for Representation: Techniques to represent negative numbers in binary.

Operations: Used in arithmetic operations to handle negative numbers.

Binary Codes:

Gray Code: A binary code where consecutive numbers differ by only one bit.

BCD (Binary Coded Decimal): Represents each decimal digit with a fixed number of binary bits.

Binary Storage and Registers:

Memory Units: Storage of binary data in memory units (RAM, ROM, etc.).

Registers: Temporary storage units used in CPUs for data manipulation.

Algebra

Boolean Algebra:

Variables: Operates on variables that can have only two values, typically denoted as 0 (false) and 1 (true).

Operations: Involves logical operations such as AND, OR, NOT, XOR, etc.

Laws and Theorems of Boolean Algebra:

Idempotent Law: $A \text{ OR } A = A$; $A \text{ AND } A = A$.

Commutative Law: $A \text{ OR } B = B \text{ OR } A$; $A \text{ AND } B = B \text{ AND } A$.

Distributive Law: $A \text{ AND } (B \text{ OR } C) = (A \text{ AND } B) \text{ OR } (A \text{ AND } C)$.

Properties of Boolean Algebra:

Associative Property: $(A \text{ OR } B) \text{ OR } C = A \text{ OR } (B \text{ OR } C)$.

De Morgan's Laws: $\text{NOT}(A \text{ AND } B) = \text{NOT } A \text{ OR } \text{NOT } B$; $\text{NOT}(A \text{ OR } B) = \text{NOT } A \text{ AND } \text{NOT } B$.

Simplification of Boolean Functions:

Karnaugh Maps: Visual method for simplifying Boolean expressions by grouping adjacent 1s. Sum-of-Products and Product-of-Sums:

Sum-of-Products: Expression in which variables are ANDed together and then ORed. Product-of-Sums: Expression in which variables are ORed together and then ANDed. Karnaugh Map:

Graphical Method: Represents truth tables in a grid to identify patterns for simplification. Minterm and Maxterm Canonical Forms:

Minterm: Represents each row in a truth table where the output is 1. Maxterm: Represents each row in a truth table where the output is 0. Don't Care Conditions:

Unused Outputs: Conditions where the output value is irrelevant for certain input combinations.