

## Unit IV

**AVL Trees, Definition, Heights of an AVL Tree, Operations-Insertion, Deletion and Searching. B-**

**Trees of order m, height of a B-Tree, insertion, deletion and searching, Comparison of Search Trees**

**Graphs: Basic terminology, representations of graphs, graph search methods DFS, BFS. Text**

**Processing: Pattern matching algorithms-Brute force, the Boyer Moore algorithm, the Knuth-Morris-**

**Pratt algorithm, Rabin Karp algorithm.**

### AVL Trees

#### 1. Definition:

- **Self-Balancing Binary Search Trees:** Maintains a balance factor to ensure logarithmic time complexity for operations.
- **Balanced Condition:** Heights of the left and right subtrees differ by at most one.

#### 2. Heights of an AVL Tree:

- **Balanced Property:** Ensuring the tree remains balanced.
- **Balancing Operations:** Rotations to maintain balance during insertions and deletions.

#### 3. Operations:

- **Insertion:** Ensuring the balance factor remains within acceptable limits.
- **Deletion:** Adjusting the tree while maintaining the balance.
- **Searching:** Leveraging the tree's balanced nature for efficient searches.

### B-Trees

#### 1. Definition of B-Trees of Order m:

- **Balanced Tree Structure:** A self-balancing tree designed for disk storage and databases.
- **Properties:** Nodes can have more than two children, reducing disk access.

#### 2. Height of a B-Tree:

- **Optimal Height:** Ensuring an efficient tree structure for disk access.

#### 3. Operations:

- **Insertion:** Maintaining B-Tree properties while accommodating new elements.
- **Deletion:** Adjusting the tree while maintaining the order and balance.

- **Searching:** Leveraging B-Tree properties for efficient searches in disk-based storage.

## Comparison of Search Trees

### 1. Comparative Analysis:

- **Efficiency Comparison:** Analyzing the performance of various search trees.
- **Trade-offs:** Considering factors like insertion, deletion, search times, memory usage, etc.

## Graphs

### 1. Basic Terminology:

- **Vertices and Edges:** Elements and connections in a graph structure.
- **Directed and Undirected Graphs:** Presence or absence of direction in edges.

### 2. Representations of Graphs:

- **Adjacency Matrix:** Representing connections between vertices.
- **Adjacency List:** Storing connections as linked lists.

### 3. Graph Search Methods:

- **Depth-First Search (DFS):** Traversing graph structures depth-wise.
- **Breadth-First Search (BFS):** Exploring nodes level by level.

## Text Processing

### 1. Pattern Matching Algorithms:

- **Brute Force:** Directly comparing a pattern with substrings.
- **Boyer Moore Algorithm:** Utilizes heuristic to jump in the search space.
- **Knuth-Morris-Pratt Algorithm:** Utilizes a pattern's own information to avoid unnecessary comparisons.
- **Rabin Karp Algorithm:** Utilizes hashing for efficient pattern searching.

### 1. AVL Trees

Definition and Properties:

AVL Trees are self-balancing binary search trees where the height difference between the left and right subtrees (balance factor) of any node is at most 1.

Heights of an AVL Tree:

The height of an AVL tree is approximately  $\log_2(n)$ , where  $n$  is the number of nodes in the tree.

Operations: Insertion, Deletion, Searching

Insertion: Ensures the tree remains balanced by performing rotations to maintain AVL properties.

Deletion: Balances the tree by performing rotations after deletion.

Searching: Follows the standard BST search algorithm.

```
// Example: AVL Tree operations
class AVLTree {
    public:
        void insert(int value) { /* ... */ }
        void remove(int value) { /* ... */ }
        bool search(int value) { /* ... */ }
};
```

## 2. B-Trees of Order $m$

Definition and Properties:

B-Trees are balanced tree structures with a variable number of children per node, designed to work well with secondary storage.

Height of a B-Tree:

The height of a B-Tree is logarithmic and depends on the number of keys and the order of the tree.

Operations: Insertion, Deletion, Searching

Insertion: Maintains B-Tree properties by redistributing keys and splitting nodes if necessary.

Deletion: Ensures B-Tree properties are preserved by merging nodes or redistributing keys.

Searching: Uses a similar mechanism as in BSTs but traverses multiple levels due to multiple children.

## 3. Comparison of Search Trees

Comparison Factors:

Comparison of search trees involves analyzing factors like the average case and worst-case time complexity of operations (searching, insertion, deletion), memory usage, and structural properties.

## 4. Graphs

Basic Terminology and Representations:

Graphs consist of vertices (nodes) and edges (connections between nodes).

Graph Search Methods: DFS, BFS

DFS (Depth-First Search): Traverses as far as possible along each branch before backtracking.

BFS (Breadth-First Search): Explores all the vertices at the present depth before moving on to the vertices at the next depth level.

### 4. Text Processing: Pattern Matching Algorithms

Brute Force, Boyer Moore, Knuth-Morris-Pratt, Rabin-Karp

Brute Force: Compares the pattern to each substring of the text.

Boyer Moore: Skips comparisons based on a "bad character" heuristic.

Knuth-Morris-Pratt: Utilizes a "failure function" to skip unnecessary comparisons.

Rabin-Karp: Uses hashing to compare the pattern with substrings of the text.